

Application of Optimization-based Energy Management Systems for Interconnected District Heating Networks

22nd Styrian Workshop on Automatic Control

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Agenda

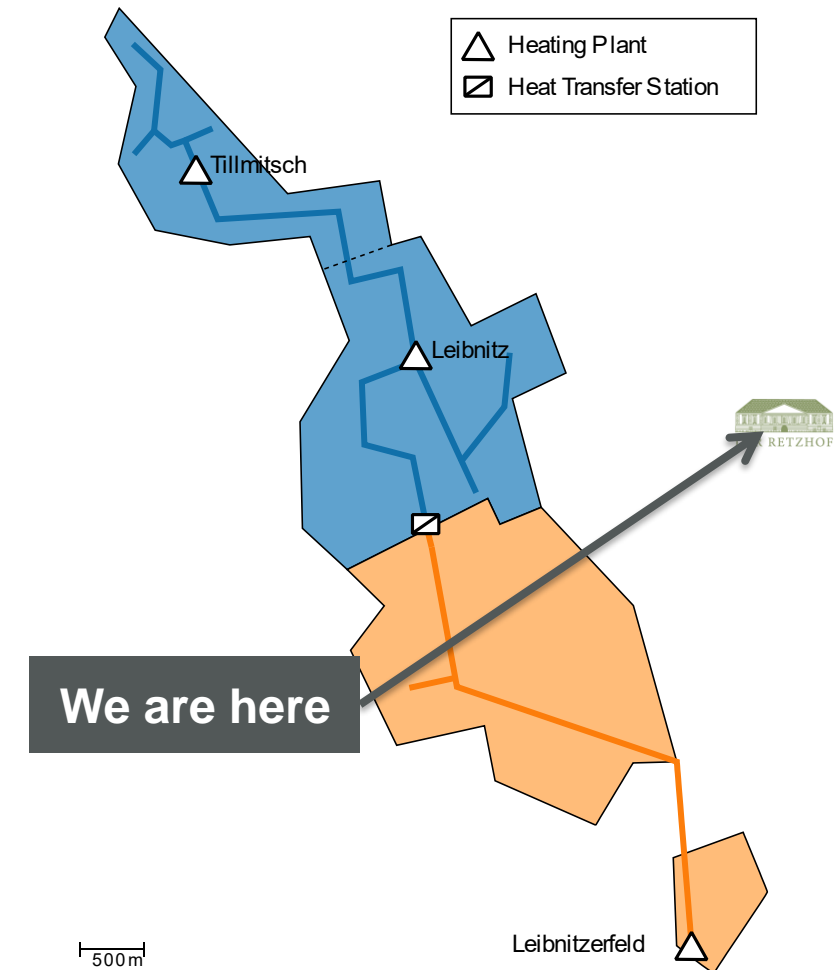
- Project Overview and Motivation
- Representation of Thermal Systems in Energy Management System (EMS)
- Handling Low-Level Controllers
- Hybrid Coupling of Energy Systems
- Results

Motivation

Project ThermaFLEX

- **Interconnected DH networks** at and around Leibnitz
 - Different production technologies, costs, storage sizes, waste heat potential,...
 - Bidirectional heat transfer
- **Goal**
 - **Minimization of CO₂ emissions/costs**
 - High-level coordination of all networks

**Optimization-based
Energy Management System**



<https://greenenergylab.at/projects/100-renewable-district-heating-leibnitz/>

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Motivation

Energy Management System (EMS)

- What we mean with energy management system (EMS)?
 - **Supervisory controller** coordinating producers, storage and consumers in an energy network



- Applications
 - Building energy management
 - Control of district heating (DH) networks
 - ...





Motivation

Optimization-based EMS

- **Prosumers**
Models the physical behavior and constraints
- **Connections**
Ensures conservation of mass and energy
- **MPC problem**

$$\min_{\mathbf{x}_i \in \mathcal{X}_i} \sum_{i=1}^N f_i(\mathbf{x}_i)$$

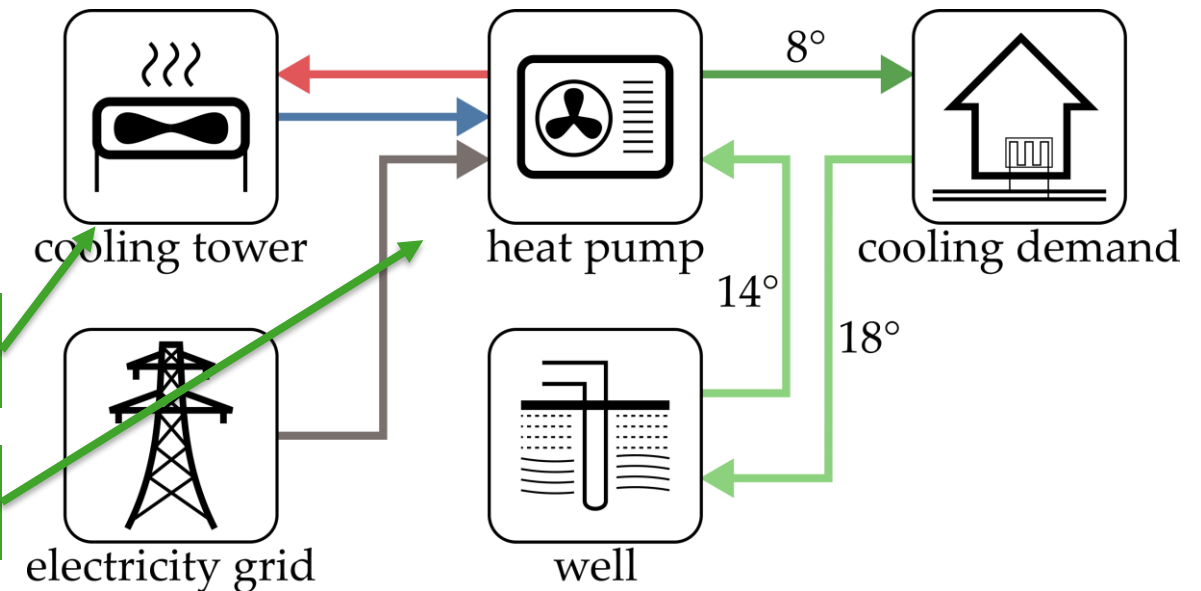
subject to

$$\sum_{i=1}^N \mathbf{A}_i \mathbf{x}_i = \mathbf{b}$$

Prosumers

Connections

In our case a MILP





Motivation

Challenges

- **Representing thermal systems in an MPC**
Temperature levels are important
- **Dealing with low-level controllers**
EMS is often only added during a retrofit
and only able to control a subset of the production units
- **Non-cooperative coupling**
Typically multi-owner setting for interconnected DH networks



Representation of Thermal Systems in EMS



Representation of Thermal Systems for EMS

Motivation: Simple boiler model

- Typical EMS only consider energy flows
 - In the case of thermal energy this means constant temperatures

$$\dot{Q}(t) = c_p \dot{m}(t) (T_{\text{in}} - T_{\text{out}})$$

- In reality the temperatures vary; model is **non-linear**

$$\dot{Q}(t) = c_p \dot{m}(t) (T_{\text{in}}(t) - T_{\text{out}})$$

If outlet is controlled at e.g. 90 °C

- Solution: “multi-temperature” model; model is **still linear**

$$\dot{Q}(t) = \sum_i c_p \dot{m}_{\text{in},i}(t) T_{\text{in},i} + c_p \dot{m}_{\text{out}}(t) T_{\text{out}} \quad \dot{m}_{\text{in},i}(t) \in \text{SOS2}$$

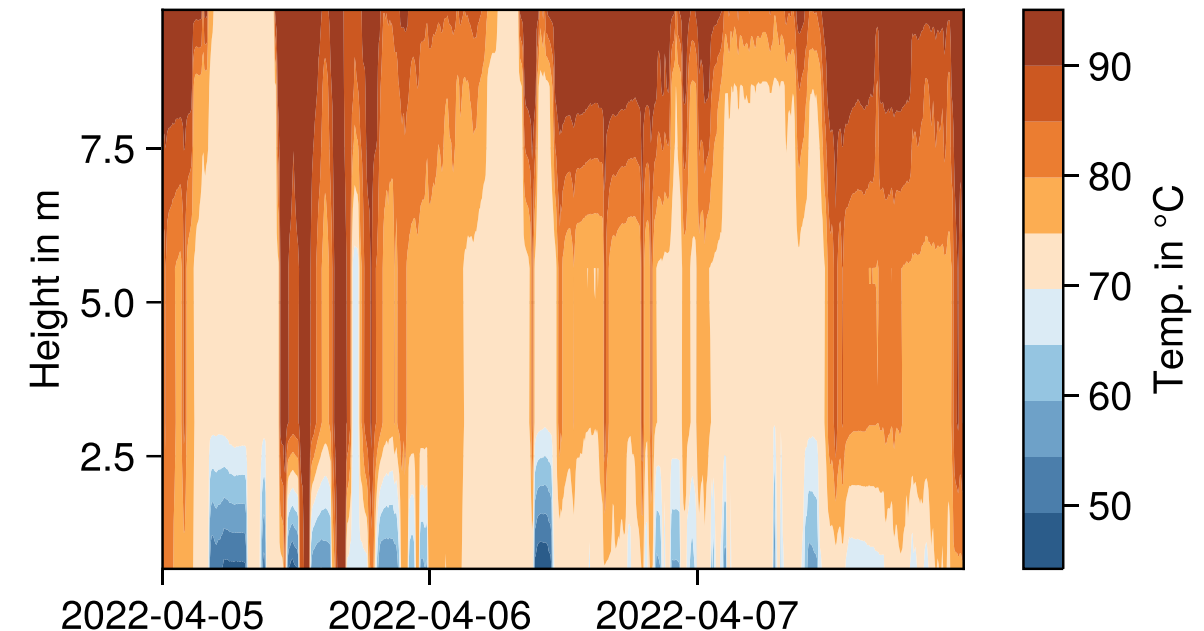


Representation of Thermal Systems for EMS

Thermal Energy Storage (TES) Model

- The constant temp. model would only allow for two layers (hot and cold)
- In reality no ideal stratification between a hot and cold layer
- Does not fit well with const. temp. model

This is a problem if we have low-level controllers that operate on temperatures





Representation of Thermal Systems for EMS

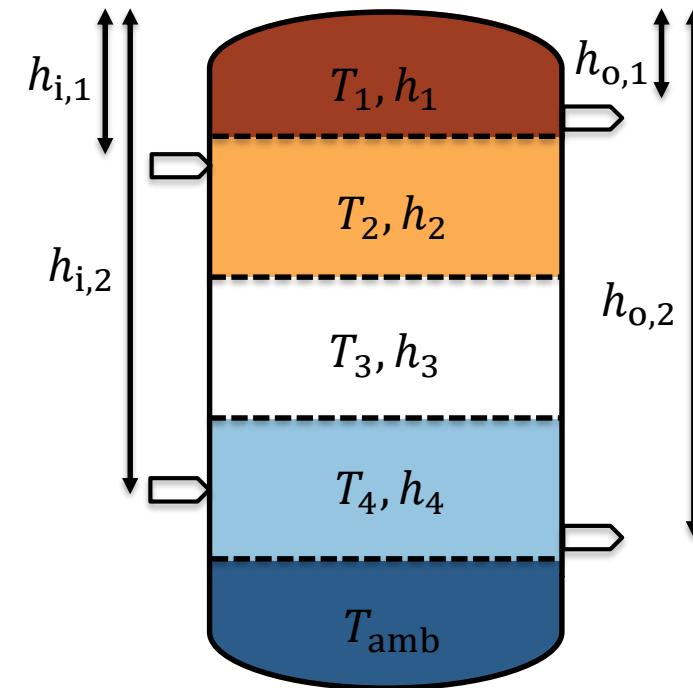
Thermal Energy Storage (TES) Model

Idea [1]

- Layers of constant temperature T_i
- States: Layer heights h_i

Accurately represent temp. distribution in TES in MILP

Why do we need this level of detail?
e.g. accurately predicting low-level TES controllers



[1] Muschick, D., Zlabinger, S., Moser, A., Lichtenegger, K., & Gölles, M. (2022). A multi-layer model of stratified thermal storage for MILP-based energy management systems. *Applied Energy*, 314, 118890.

<https://doi.org/10.1016/j.apenergy.2022.118890>



Handling Low-Level Controllers





Handling Low-Level Controllers

Motivation

- EMS is often only added during a **retrofit**
- EMS may at first be only allowed to...
 - provide **optimal setpoints** for low-level controllers
 - control a **subset of the production units**
- Needs to **gain trust** first

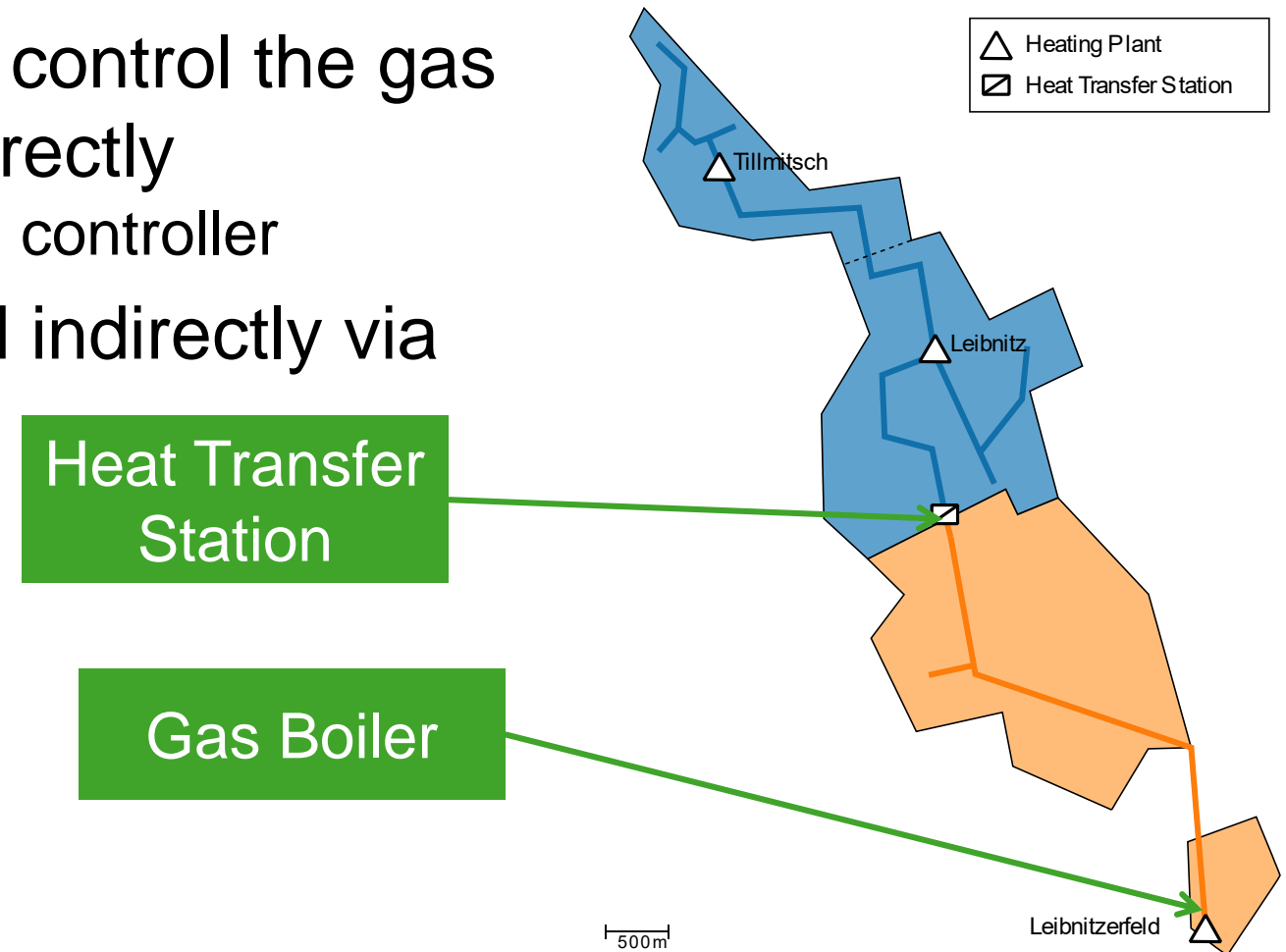
Represent low-level
controllers in EMS



Handling Low-Level Controllers

Motivation

- EMS was not allowed to control the gas boiler in Leibnitzerfeld directly
Still controlled via a low-level controller
- Could only be influenced indirectly via the imported heat





Handling Low-Level Controllers

Motivation

- Low-level controllers are very often “simple” but **highly non-linear**
 - Two-point controller
 - PI with anti-windup
 - IF-THEN-ELSE logic
- How to represent them in a **MILP** optimization problem?
 - Mixed logical-dynamical system [1]

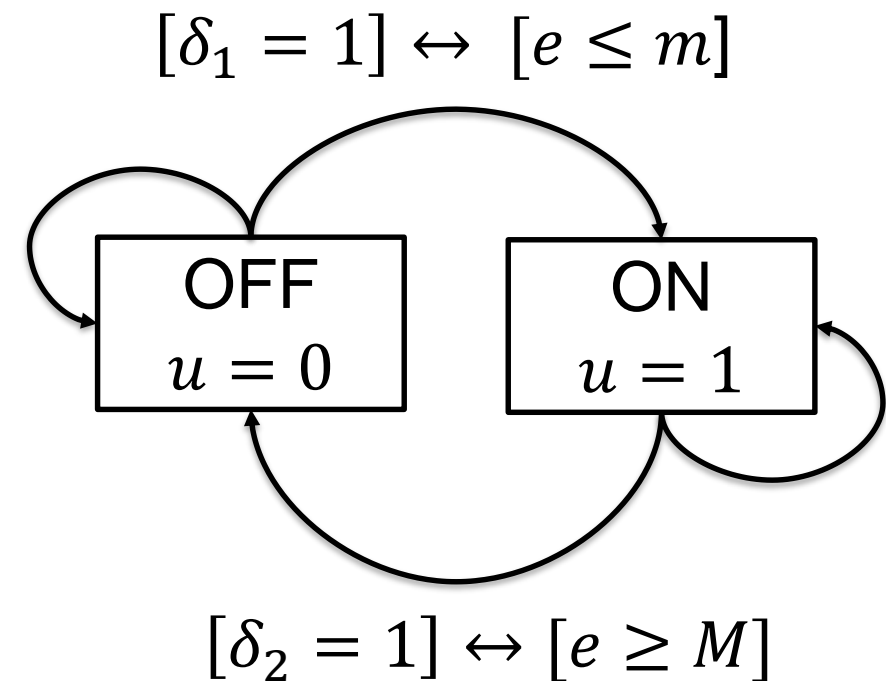
[1] Bemporad, A., & Morari, M. (1999). Control of systems integrating logic, dynamics, and constraints. *Automatica*, 35(3), 407–427. [https://doi.org/10.1016/S0005-1098\(98\)00178-2](https://doi.org/10.1016/S0005-1098(98)00178-2)



Handling Low-Level Controllers

Example: Two-Point Controller with hysteresis

- “When are we in state ON?”
- $[u_{k+1}] \leftrightarrow [(\neg u_k \wedge \delta_{1,k}) \vee (u_k \wedge \neg \delta_{2,k})]$
- MILP formulation?
- **Idea** (logic to inequality):
 - $\delta_1 \vee \delta_2$ is equivalent to $\delta_1 + \delta_2 \geq 1$
 - $\delta_1 \vee \neg \delta_2$ is equivalent to $\delta_1 + (1 - \delta_2) \geq 1$
- Convert to CNF and incorporate as inequality constraints





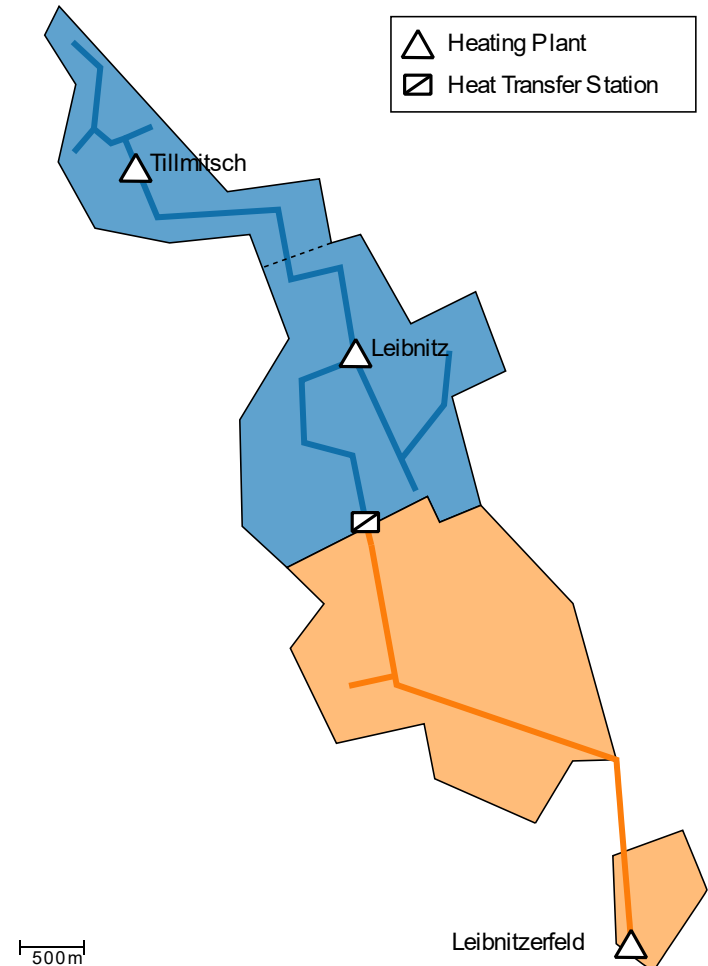
Hybrid Coupling of Energy Systems



Hybrid Coupling of Energy Systems

Motivation

- Control of **interconnected DH networks** with different owners
- **Different economic interests** (non-cooperative)
- Global (social) optimum, not adequate
- **Mixture** of cooperative and non-cooperative coupling; “Coalitions”





Hybrid Coupling of Energy Systems

Mathematical Representation

Cooperative coupling

- Each agent has local constraints and a local objective function
- Agents minimize the global objective function

$$\min_{\mathbf{x}_i \in \mathcal{X}_i} \sum_{i=1}^N f_i(\mathbf{x}_i)$$

subject to $\sum_{i=1}^N \mathbf{A}_i \mathbf{x}_i = \mathbf{b}$

One opt. problem
Social optimum

Non-cooperative coupling

- Each agent has local constraints and a local objective function
- Each agent minimizes only its local cost function

$$\min_{\mathbf{x}_i \in \mathcal{X}_i} f_i(\mathbf{x}_i), \quad i = 1, \dots, N$$

subject to $\sum_{i=1}^N \mathbf{A}_i \mathbf{x}_i = \mathbf{b}$

N coupled opt. problems
Nash equilibrium



Hybrid Coupling of Energy Systems

Mathematical Representation – Cooperative Coupling

$$\begin{aligned} \min_{\mathbf{x}_i \in \mathcal{X}_i} \quad & \sum_{i=1}^N f_i(\mathbf{x}_i) \\ \text{subject to} \quad & \sum_{i=1}^N \mathbf{A}_i \mathbf{x}_i = \mathbf{b} \end{aligned}$$

- Separable Programme
- Solution is **social optimum**

Apply augmented
Lagrangian method

- Augmented Lagrange function

$$\begin{aligned} \mathcal{L}(\mathbf{x}, \boldsymbol{\lambda}) = & \sum_{i=1}^N f_i(\mathbf{x}_i) + \boldsymbol{\lambda}^T \left(\sum_{i=1}^N \mathbf{A}_i \mathbf{x}_i - \mathbf{b} \right) \\ & + \frac{\rho}{2} \left\| \sum_{i=1}^N \mathbf{A}_i \mathbf{x}_i - \mathbf{b} \right\|_2^2 \end{aligned}$$

- Dual ascent

$$\mathbf{x}_i^{(k+1)} = \underset{\mathbf{x}_i \in \mathcal{X}_i}{\operatorname{argmin}} \mathcal{L}_i \left(\mathbf{x}_i, \boldsymbol{\lambda}^{(k)}, \mathbf{x}_{-i}^{(k)} \right)$$

$$\boldsymbol{\lambda}^{(k+1)} = \boldsymbol{\lambda}^{(k)} + \rho \left(\sum_{i=1}^N \mathbf{A}_i \mathbf{x}_i^{(k+1)} - \mathbf{b} \right)$$



Hybrid Coupling of Energy Systems

Mathematical Representation – Non-cooperative coupling

$$\begin{aligned} \min_{\mathbf{x}_i \in \mathcal{X}_i} \quad & f_i(\mathbf{x}_i), \quad i = 1, \dots, N \\ \text{subject to} \quad & \sum_{i=1}^N \mathbf{A}_i \mathbf{x}_i = \mathbf{b} \end{aligned}$$

- N-player game
- Solution is a **Nash equilibrium**

N coupled opt. problems

Apply augmented Lagrangian method for each

- Augmented Lagrange functions

$$\begin{aligned} \mathcal{L}_i(\mathbf{x}_i, \boldsymbol{\lambda}_i) = & f_i(\mathbf{x}_i) + \boldsymbol{\lambda}_i^T \left(\mathbf{A}_i \mathbf{x}_i + \sum_{j \neq i} \mathbf{A}_j \mathbf{x}_j - \mathbf{b} \right) \\ & + \frac{\rho}{2} \left\| \mathbf{A}_i \mathbf{x}_i + \sum_{j \neq i} \mathbf{A}_j \mathbf{x}_j - \mathbf{b} \right\|_2^2 \end{aligned}$$

- Dual ascent

$$\mathbf{x}_i^{(k+1)} = \operatorname{argmin}_{\mathbf{x}_i \in \mathcal{X}_i} \mathcal{L}_i(\mathbf{x}_i, \boldsymbol{\lambda}_i^{(k)}, \mathbf{x}_{-i}^{(k)})$$

$$\boldsymbol{\lambda}_i^{(k+1)} = \boldsymbol{\lambda}_i^{(k)} + \rho \left(\mathbf{A}_i \mathbf{x}_i^{(k+1)} + \sum_{j \neq i} \mathbf{A}_j \mathbf{x}_j^{(k)} - \mathbf{b} \right)$$



Hybrid Coupling of Energy Systems

Mathematical Representation - Comparison

ALM for cooperative coupling

ALM for non-coop. coupling

$$\mathbf{x}_i^{(k+1)} = \operatorname{argmin}_{\mathbf{x}_i \in \mathcal{X}_i} \mathcal{L}(\mathbf{x}_i, \boldsymbol{\lambda}^{(k)}, \mathbf{x}_{-i}^{(k)})$$

$$\mathbf{x}_i^{(k+1)} = \operatorname{argmin}_{\mathbf{x}_i \in \mathcal{X}_i} \mathcal{L}_i(\mathbf{x}_i, \boldsymbol{\lambda}_i^{(k)}, \mathbf{x}_{-i}^{(k)})$$

$$\boldsymbol{\lambda}^{(k+1)} = \boldsymbol{\lambda}^{(k)} + \rho \left(\sum_{i=1}^N \mathbf{A}_i \mathbf{x}_i^{(k+1)} - \mathbf{b} \right)$$

$$\boldsymbol{\lambda}_i^{(k+1)} = \boldsymbol{\lambda}_i^{(k)} + \rho \left(\mathbf{A}_i \mathbf{x}_i^{(k+1)} + \sum_{j \neq i} \mathbf{A}_j \mathbf{x}_j^{(k)} - \mathbf{b} \right)$$

Very similar \Rightarrow Idea: Combination
for hybrid coupling



Hybrid Coupling of Energy Systems

Mathematical Representation – Hybrid Coupling

$$\mathbf{x}_i^{(k+1)} = \operatorname{argmin}_{\mathbf{x}_i \in \mathcal{X}_i} \mathcal{L} \left(\mathbf{x}_i, \mathbf{x}_{j \neq i}^{(k)}, \boldsymbol{\lambda}_i^{(k)} \right)$$

$$\boldsymbol{\lambda}_{i,c}^{(k+1)} = \boldsymbol{\lambda}_{i,c}^{(k)} + \rho \left(\mathbf{A}_i \mathbf{x}_i^{(k+1)} + \sum_{j \neq i}^N \mathbf{A}_i \mathbf{x}_j^{(k)} - \mathbf{b} \right), \quad i = 1, \dots, N, \quad c \in \mathcal{C}_{\text{non-coop}}$$

$$\boldsymbol{\lambda}_{i,c}^{(k+1)} = \boldsymbol{\lambda}_{i,c}^{(k)} + \rho \left(\mathbf{A}_i \mathbf{x}_i^{(k+1)} + \sum_{j \neq i}^N \mathbf{A}_i \mathbf{x}_j^{(k+1)} - \mathbf{b} \right), \quad i = 1, \dots, N, \quad c \in \mathcal{C}_{\text{coop}}$$

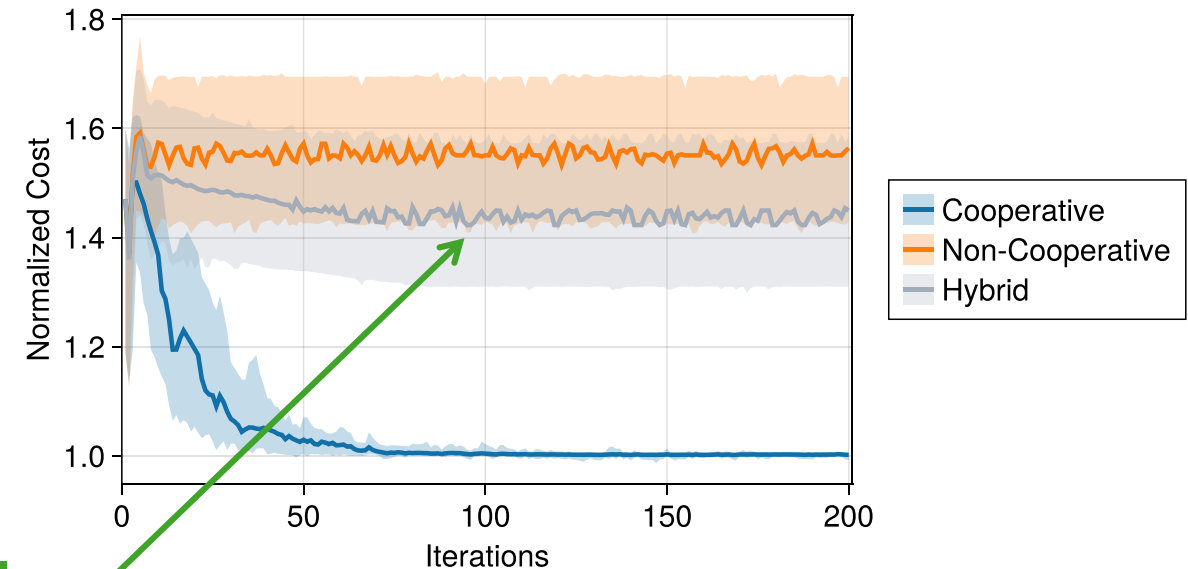
V. Kaisermayer, D. Muschick, M. Horn, and M. Göllés, “Operation of Coupled Multi-Owner District Heating Networks via Distributed Optimization,” *Energy Reports*, vol. 7, pp. 273–281, Oct. 2021.



Hybrid Coupling of Energy Systems Simulation Study

Test Problems

- All three grids **cooperative**
- All three grids **non-cooperative**
- The two grids that belong to the same owner cooperate; the third does not (**hybrid**)



Shaded area is range of solutions for different input datasets



Real Operation

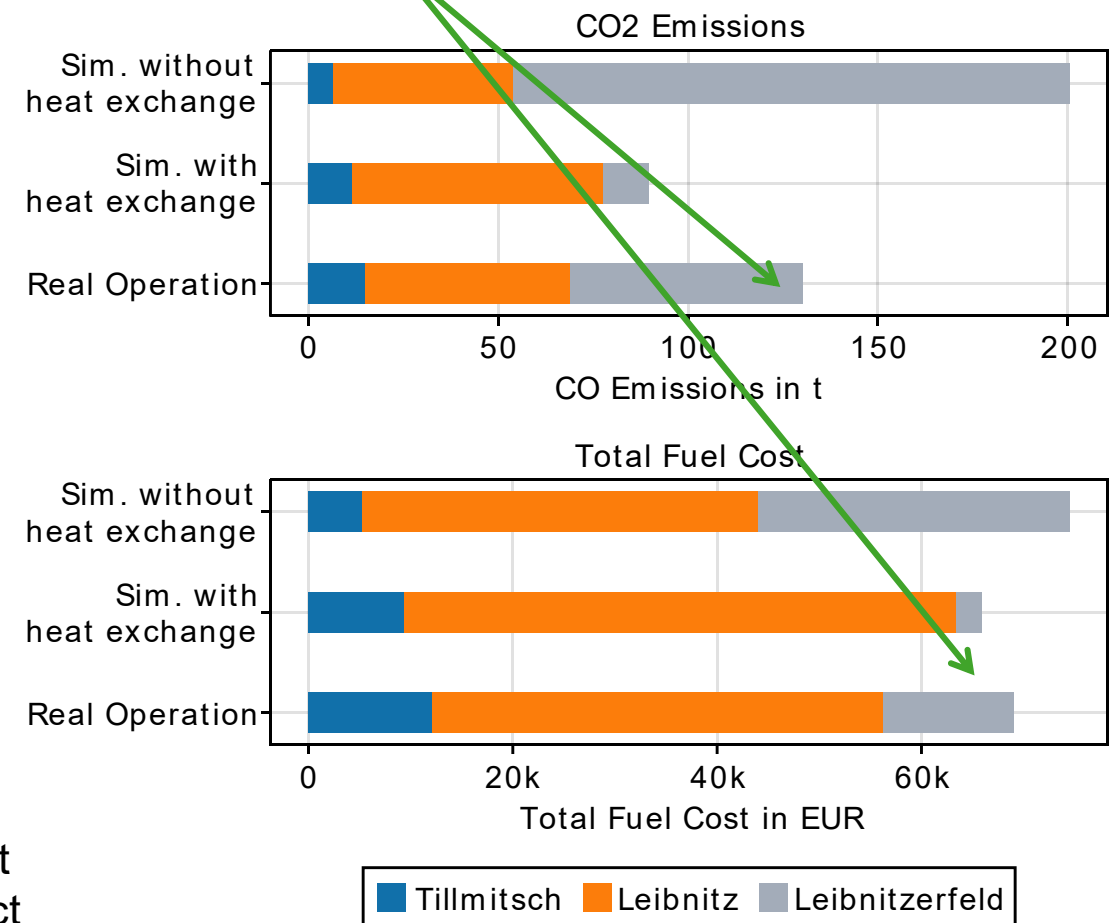




Real Operation Pre-Simulation Study

35% reduction in CO₂ emissions
7% fuel cost reduction
during 1 month (April 2021)

- **Cooperative EMS** was implemented
 - “Fair” contract between owners
- Simulation study as a best-case scenario
 - With and without (base case) heat exchanger
- Real operation



V. Kaisermayer *et al.*, “Smart control of interconnected district heating networks on the example of ‘100% Renewable District Heating Leibnitz,’” *Smart Energy*, vol. 6, May 2022.

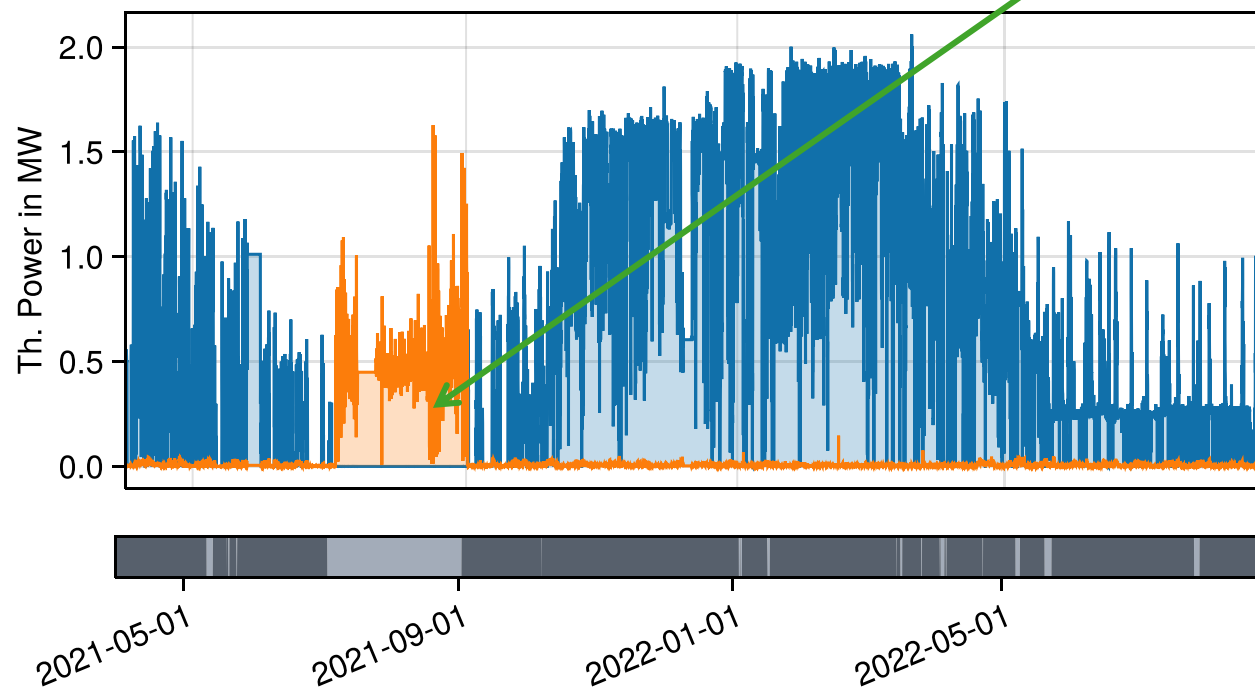


Real Operation Heat Transfer Station

Maintenance during summer

- **Running since April 2021**

Saved 7537 MWh of gas boiler operation
About* 1,9 Mt of CO₂



From Leibnitz to Leibnitzerfeld
From Leibnitzerfeld to Leibnitz

EMS not active
EMS active

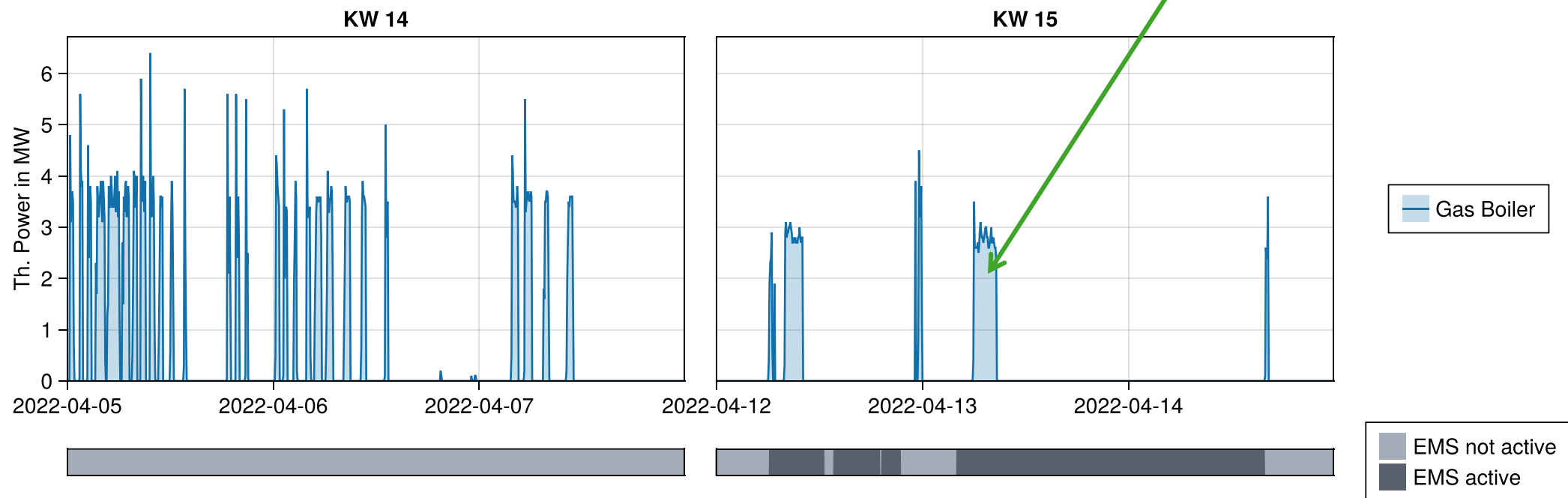
* 0,201 tCO₂/MWh @ 80% efficiency



Real Operation Gas Boiler Operation

- During KW15 the EMS was given full control

Reduced Gas Boiler Operation by 70%
Better Operating Conditions:
(longer run time, lower power level)



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